

Adding signals such as noise can increase the resolution of an ADC. Without the added signal, the ADC will always result in the same digital value; see for example the situation below (left):



In this example, the constant input voltage  $V_i$  will always result in the digital value n and there is thus a constant (systematic) error  $\delta V = V_i - V_n$ .

- Show that by adding a saw-tooth or triangular signal to  $V_i$  (see right figure), in combination with oversampling and averaging, the resolution can be increased.
- What is the needed amplitude and offset of the signal  $(\Delta V \equiv V_{n+1} V_n)$ ?

The above example is equivalent to adding noise with a rectangular distribution (probability P(v) to add voltage v is constant in the range defined by the amplitude and offset).

• Can the same result be achieved by adding a sine wave signal or by adding random noise? In case yes: what are the parameters (amplitude and offset)? Note: random ("white") noise has a probability density function

$$P(v) = \frac{1}{\sigma \sqrt{2\pi}} \exp\left[-\frac{v^2}{2\sigma^2}\right]$$

(for Normal Distribution, see Wikipedia: http://en.wikipedia.org/wiki/Normal\_distribution)