

1)  $R(t) = R_f + (R_i - R_f) \exp(-t/\tau)$

$R_f$ : final value =  $100 \text{ k}\Omega$

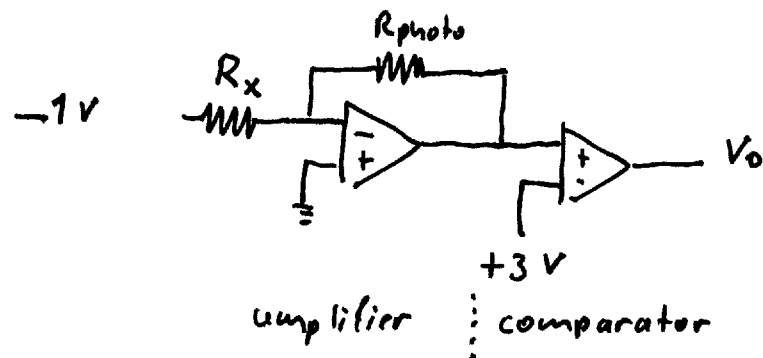
$R_i$ : initial value =  $30 \text{ k}\Omega$

$\tau = 50 \text{ ms}$

$R(t) = 100 \text{ k}\Omega - 70 \text{ k}\Omega \exp(-t/50 \text{ ms})$

$R(10 \text{ ms}) = 42.69 \text{ k}\Omega$

Example



$$(-1 \text{ V}) \times \left( - \frac{R_{photo}}{R_x} \right) = +3 \text{ V}$$

$$R_{photo} = 42.69 \text{ k}\Omega \Rightarrow R_x = 14.2 \text{ k}\Omega$$

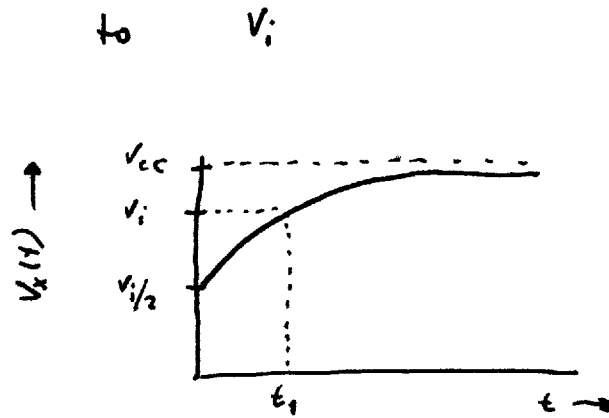
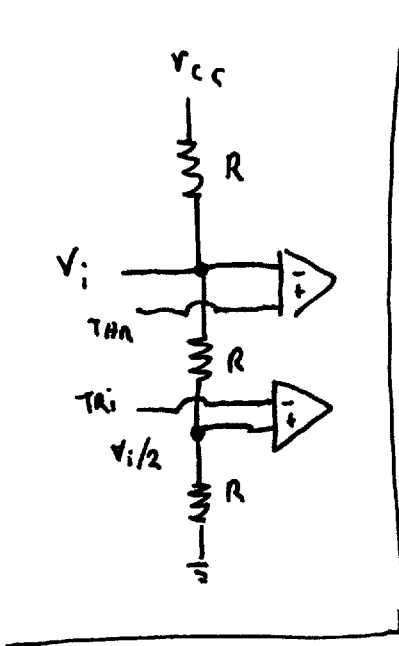
2] See lecture notes

3] This circuit is very similar to the oscillator of our exercises, with one small difference:

Instead of the control voltage of the top comparator being  $\frac{2}{3} V_{cc}$  it is at  $V_i$ , and the other  $\frac{1}{3} V_{cc} \rightarrow \frac{1}{2} V_i$

This makes the timing different. At the

capacitor charging cycle it charges from  $\frac{1}{2} V_i$



$$V_x(t) = V_{cc} - (V_{cc} - V_i/2) \exp(-t/\tau_1)$$

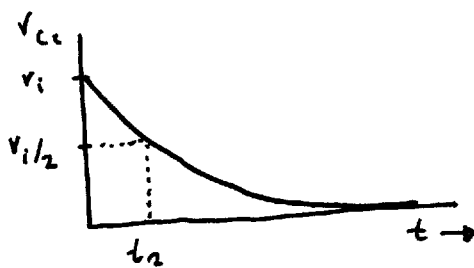
$$\tau_1 = (R_1 + R_2) C$$

When  $V_x$  reaches  $V_i$  the system commutates

$$V_{cc} - (V_{cc} - V_i/2) \exp(-t/\tau_1) = V_i$$

$$t_1 = \tau_1 \ln \left( \frac{V_{cc} - V_i/2}{V_{cc} - V_i} \right) \quad \left( \begin{array}{l} \text{note that we get} \\ \tau_1 \ln(2) \text{ back for} \\ V_i = 2/3 V_{cc} \end{array} \right)$$

For the discharging cycle we have



$$V_x(t) = V_i \exp(-t/\tau_2)$$

$$\tau_2 = R_2 C$$

When  $V_x$  reaches  $V_i/2$  the system commutates

$$V_i \exp(-t/\tau_2) = V_i/2$$

$$t_2 = \tau_2 \ln(2)$$

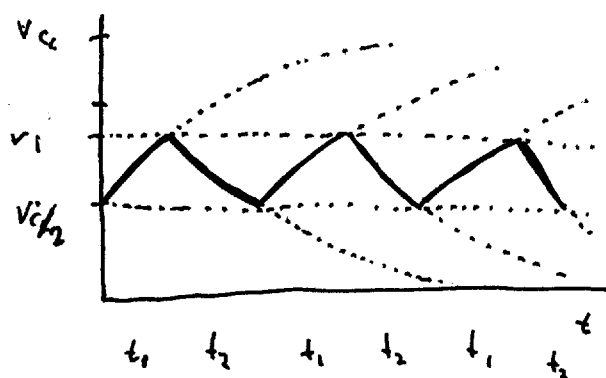
$$\left( \begin{array}{l} \text{note that this is} \\ \text{equal to case for} \\ V_i = 2/3 V_{cc} \end{array} \right)$$

The total frequency is given by

$$f = \frac{1}{t_1 + t_2} = \frac{1}{\tau_1 \ln \left( \frac{V_{cc} - V_i/2}{V_{cc} - V_i} \right) + \tau_2 \ln(2)}$$

$$= \frac{1}{(R_1 + R_2) C \ln \left( \frac{V_{cc} - V_i/2}{V_{cc} - V_i} \right) + R_2 C \ln(2)}$$

The final figure



4] See lecture notes

5] a) See lecture notes

$$B_z = \frac{1}{\gamma} \frac{V_y d}{V_x h}$$

or

$$V_y = \frac{\gamma B_z h V_x}{d}$$

b)

$$\begin{aligned} \mu &= 1500 \text{ cm}^2/\text{Vs} = 0.15 \text{ m}^2/\text{Vs} \\ h &= 1 \text{ cm} \\ d &= 1 \text{ mm} \\ V_x &= 10 \text{ V} \\ B_z &= 0.1 \text{ T} \end{aligned} \left. \vphantom{\begin{aligned} \mu &= 1500 \text{ cm}^2/\text{Vs} \\ h &= 1 \text{ cm} \\ d &= 1 \text{ mm} \\ V_x &= 10 \text{ V} \\ B_z &= 0.1 \text{ T} \end{aligned}} \right\} V_y = 1.5 \text{ V}$$

c)

$$S = \frac{dV_y}{dB_z} = \frac{\mu h V_x}{d} = 15 \text{ V/T}$$

d)

$$30 \text{ mT} \rightarrow 0.45 \text{ V} \rightarrow \text{scale } 2 \text{ volt} \rightarrow \Delta V = 0.001 \text{ V}$$

$$\Rightarrow \Delta B = \frac{\Delta V}{S} = \frac{1 \text{ mV}}{15 \text{ V/T}} = 67 \text{ } \mu\text{T}$$