

S - II - 2010

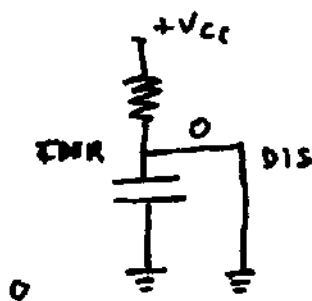
①

when a (negative) pulse is received at the trigger input (TRI), the bottom comparator goes to high



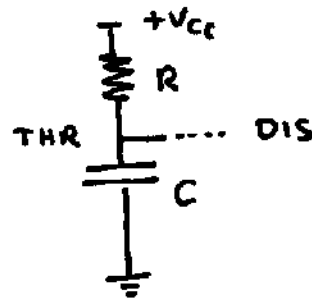
if $TRI < \frac{1}{3} V_{cc}$
 $S \rightarrow +V_{cc}$

This change low-high sets the flip flop output (out $\rightarrow +V_{cc}$) and \bar{Q} becomes low. This closes the "switch" (transistor) and the DIS line is effectively disconnected from ground. DIS \rightarrow open circuit. We now have the following situation



before

\Rightarrow



after

The capacitor C, initially discharged ($\Delta V = 0 - 0 = 0$), starts charging. Exponentially, $\tau = RC$, $V_c(t=0) = 0$, $V_c(t=\infty) = V_{cc}$.

$$V_{DIS} = V_{THR} = V_{cc} (1 - \exp(-t/RC))$$

The capacitor continues being charged until this voltage becomes larger than $V_{CON} (= \frac{2}{3} V_{cc})$

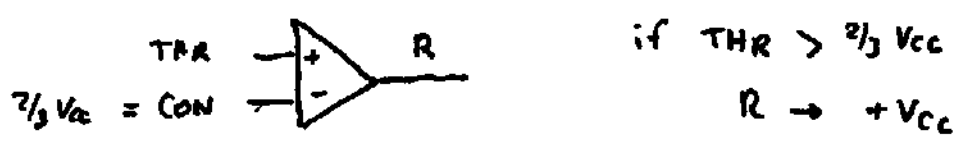
This takes place at a time when

$$V_{Dis} = V_{THR} = V_{CON}$$

$$V_{CC} (1 - \exp(-t/RC)) = \frac{2}{3} V_{CC}$$

$$\Rightarrow t = RC \ln(3)$$

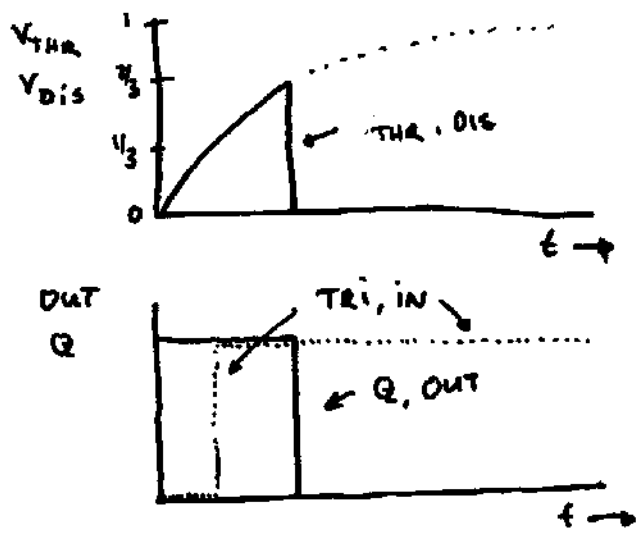
At this moment the top comparator goes from low to high



Note that the bottom comparator might still be high as well, but that is irrelevant; The flip-flop responds to changes \downarrow and not to states.

The flip-flop thus is reset. $out = Q \rightarrow 0$,

\bar{Q} goes to high and the 'switch' transistor is opened, connecting the capacitor to ground, which is thus instantaneously discharged.



b) $RC \ln(3) = 1 \text{ ms}$

ex. $C = 1 \text{ } \mu\text{F}$

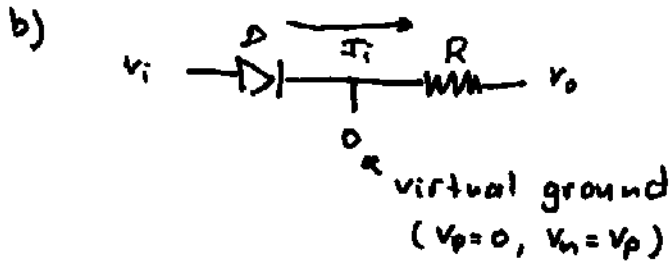
$$R = \frac{1 \text{ ms}}{1 \text{ } \mu\text{F} \ln(3)} = 910 \text{ } \Omega$$

② a) see lecture notes

- $r_{in} = \infty$

- $r_{out} = 0$

- $A = \infty \Rightarrow v_p = v_n$ (unless saturation)



$$I_i = I_0 \left[\exp\left(\frac{v_i}{V_T}\right) - 1 \right]$$

This current cannot escape but through R

$$V_o = 0 - I_i R = -R I_0 \left[\exp\left(\frac{v_i}{V_T}\right) - 1 \right]$$

c) $P_{out} = V_{out} \times I_{out} = -R I_0 \left[\exp\left(\frac{v_i}{V_T}\right) - 1 \right] \times (-I_0 \left[\exp\left(\frac{v_i}{V_T}\right) - 1 \right])$

$$= R I_0^2 \left[\exp\left(\frac{v_i}{V_T}\right) - 1 \right]^2$$

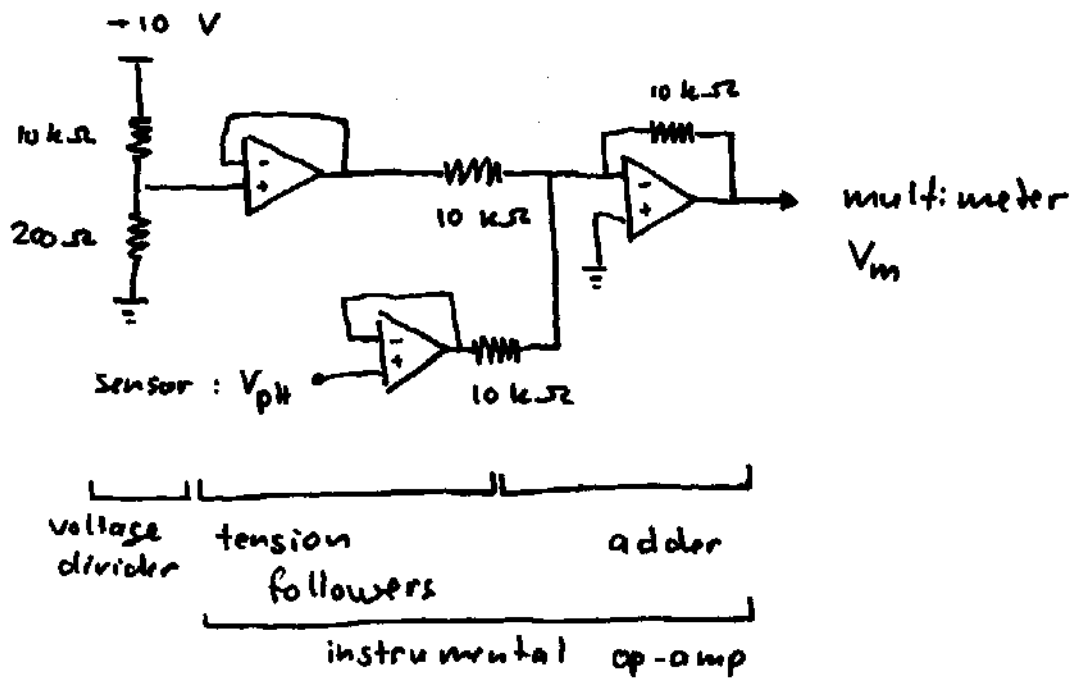
$v_i = -\infty \Rightarrow P_{out} = R I_0^2 = 10^{-26} \text{ W}$. no problem!

forward bias:

$$P_{out} \approx R I_0^2 \left[\exp\left(\frac{v_i}{V_T}\right) \right]^2 = R I_0^2 \exp\left(\frac{2v_i}{V_T}\right)$$

$P_{max} = 10 \text{ mW} \Rightarrow v_{i,max} = 0.69 \text{ V}$

- ③ a) The signal at a pH of 5 is equal to +200 mV. To get highest resolution we have to subtract this voltage.



b) $\Delta N_{H^+} = \frac{\Delta V_m}{\frac{dV_m}{dN_{H^+}}}$, $\Delta V_m = 0,01 \text{ mV}$

$$\frac{dV_m}{dN} = \frac{dV_m}{d\text{pH}} \cdot \frac{d\text{pH}}{dN} = \frac{dV_m}{dV_{pH}} \cdot \frac{dV_{pH}}{d\text{pH}} \cdot \frac{d\text{pH}}{d[N]} \cdot \frac{d[N]}{dN}$$

$$\left. \begin{aligned} \frac{dV_m}{dV_{pH}} &= 1 \quad (\text{see circuit above}) \\ \frac{dV_{pH}}{d\text{pH}} &= 100 \text{ mV} \\ \frac{d\text{pH}}{dN} &= \frac{1}{\ln(10)} \cdot \frac{1}{[N_{H^+}]} \\ \frac{d[N_{H^+}]}{dN} &= \frac{1}{3l} \end{aligned} \right\} \frac{dV_m}{dN_{H^+}} = \frac{100 \text{ mV}}{\ln(10)} \cdot \frac{1}{[N_{H^+}]} \cdot \frac{1}{3l}$$

$$\text{pH} = 5 \Rightarrow [N_{H^+}] = 10^9 / \text{liter}$$

$$\frac{dV_m}{dN_{H^+}} = 1.45 \cdot 10^{-11} \text{ V / atom } H^+$$

$$\Rightarrow \Delta N_{H^+} = \frac{10 \mu\text{V}}{1.45 \cdot 10^{-11} \text{ V}} \text{ atoms } H^+ = 6.9 \times 10^5 \text{ atoms}$$

(4)

See lecture notes

- thermo couple
 - PT 100
 - thermistor
 - diode
 - mechanical sensor
 - spectrum analyzer
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(5)

See lecture notes

