

# Control

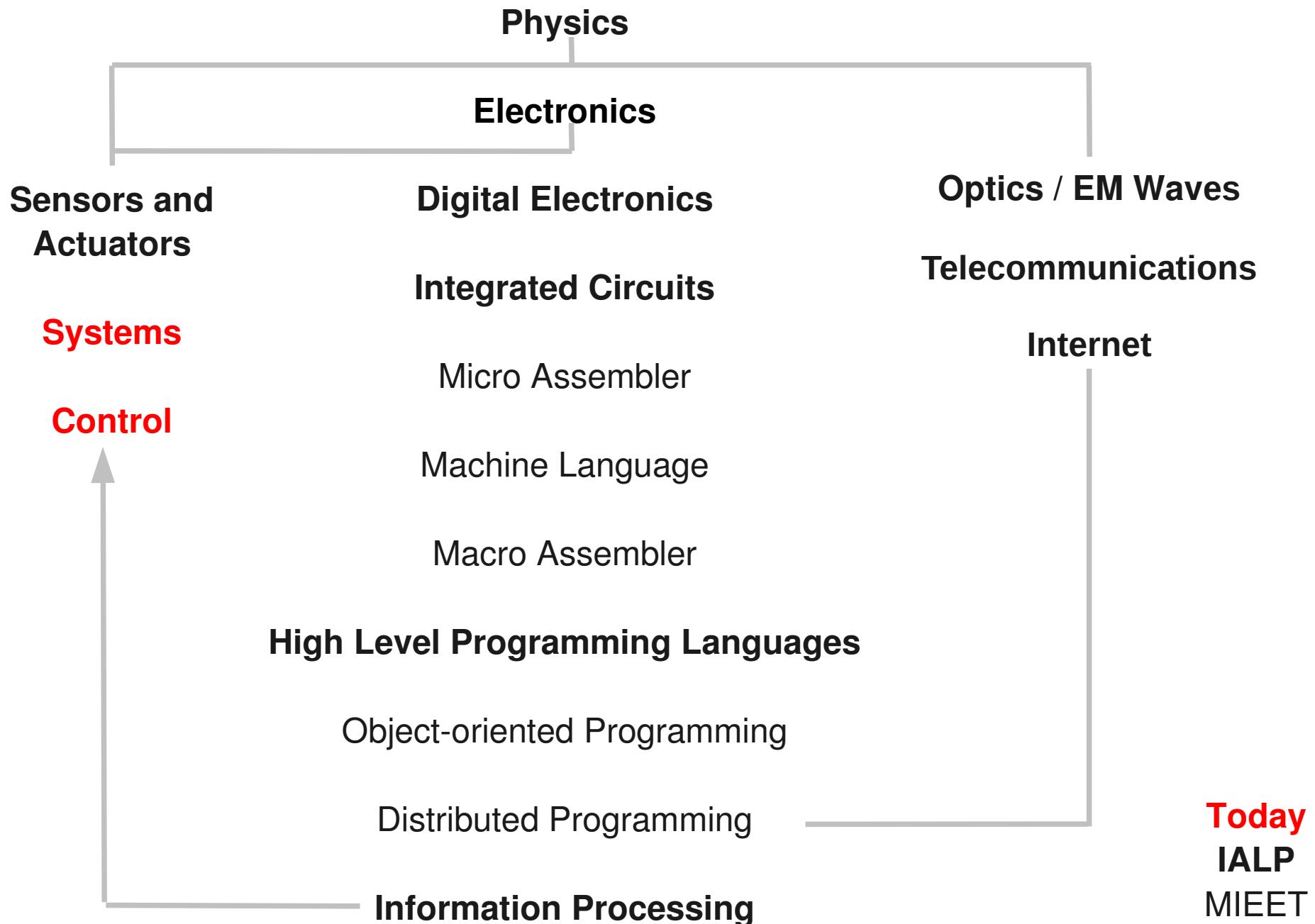
20.

MIEET 1º ano

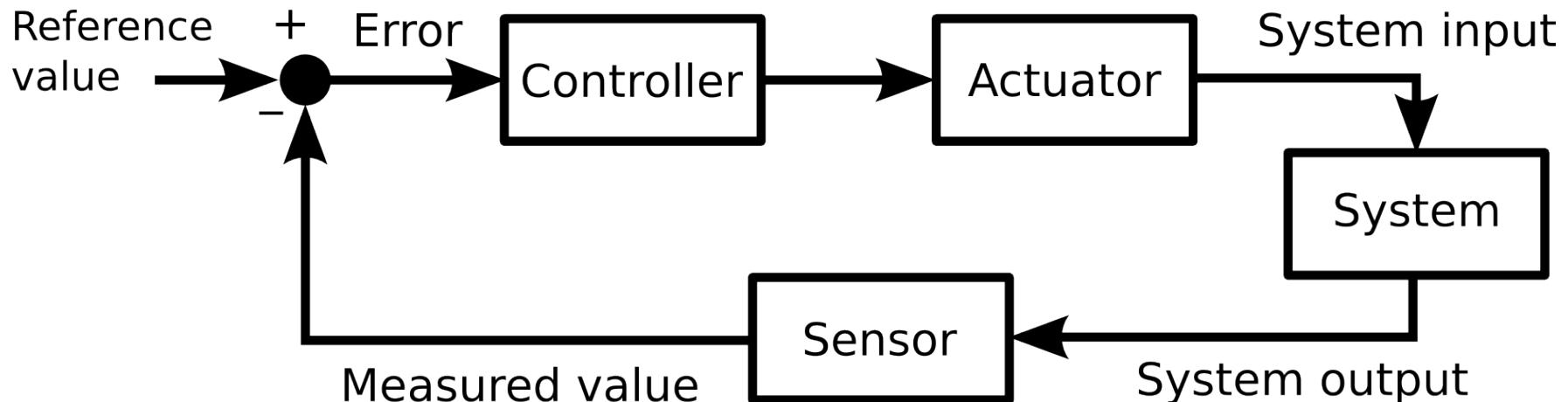


Peter Stallings, UAAlg 2011

# MIEET. The levels of knowledge



# Control theory

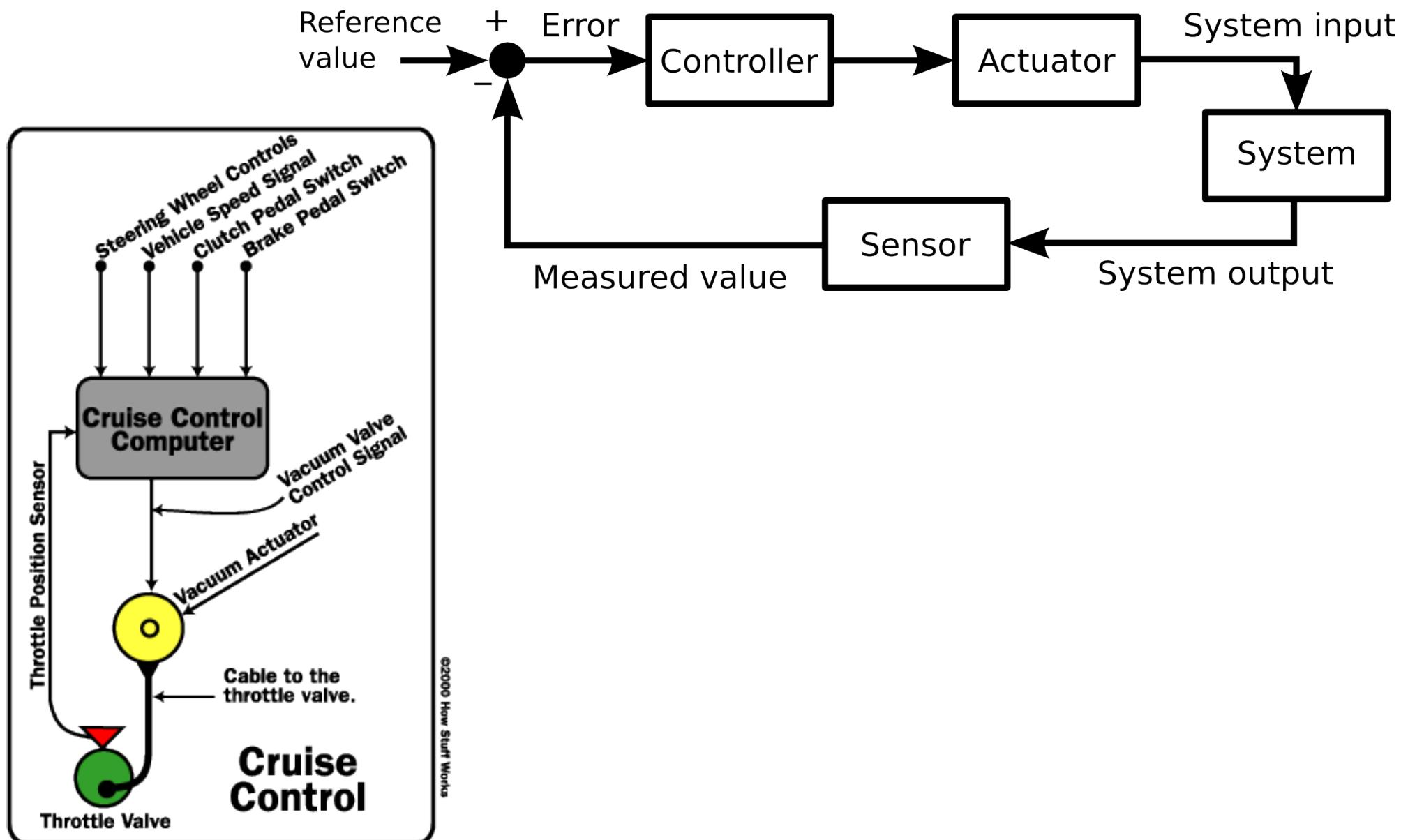


Cruise Control Symbol



Distance Control (Adaptive Cruise Control)

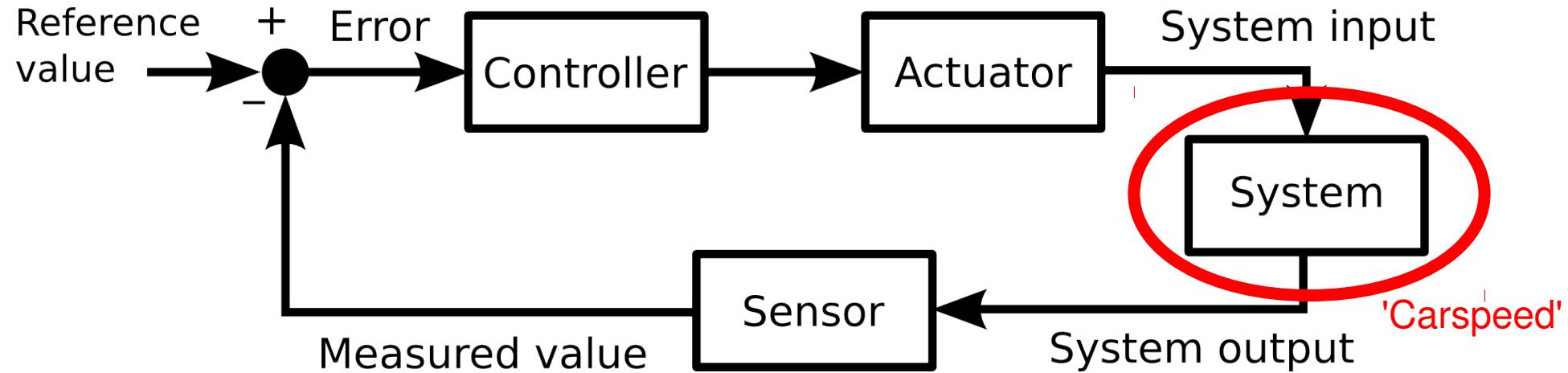
# Control theory



# Example. Cruise control



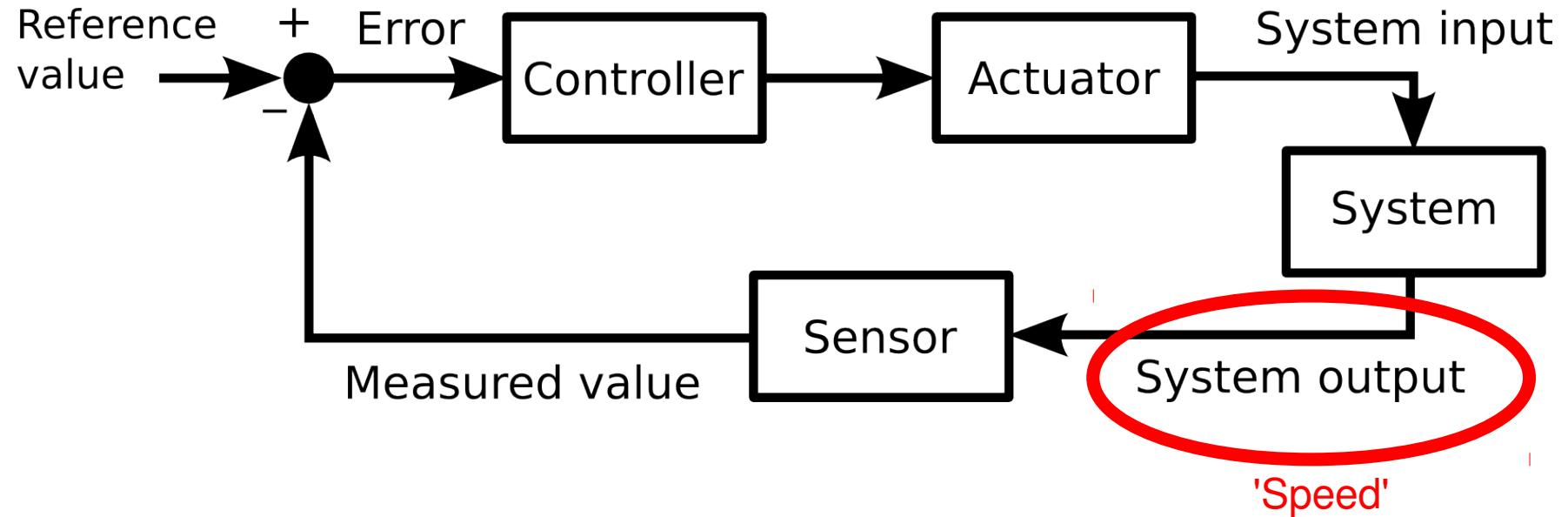
1: The 'system' we want to control



# Example. Cruise control



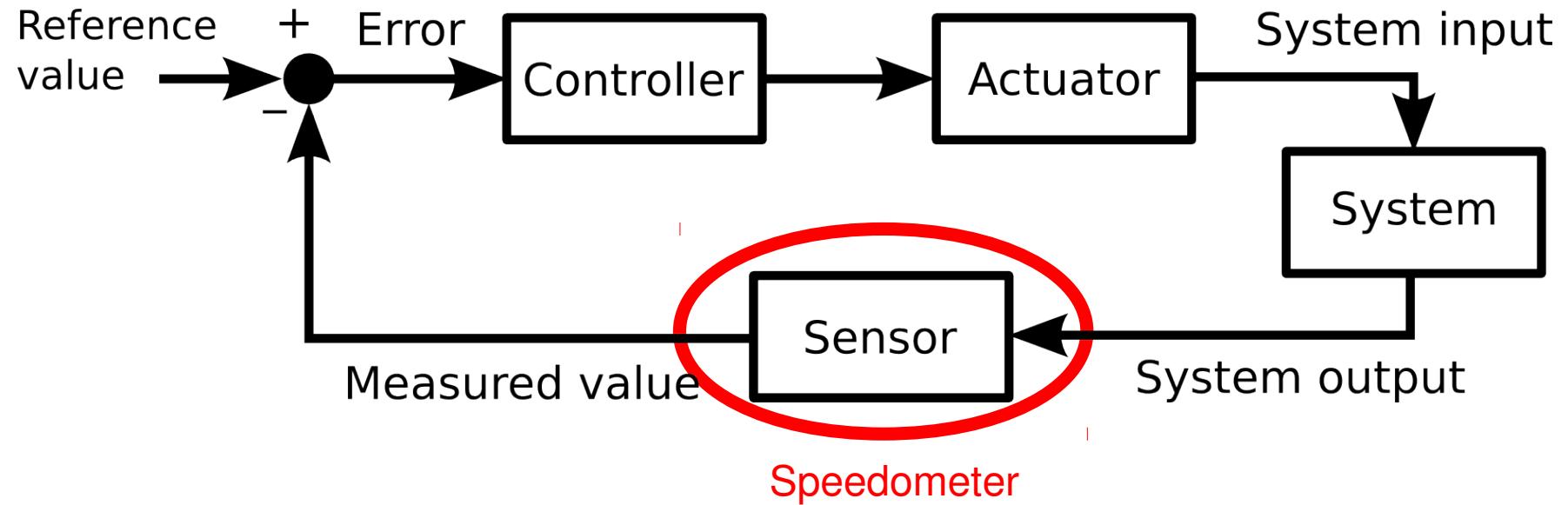
2: The 'variable' we use to monitor the state of the system



# Example. Cruise control



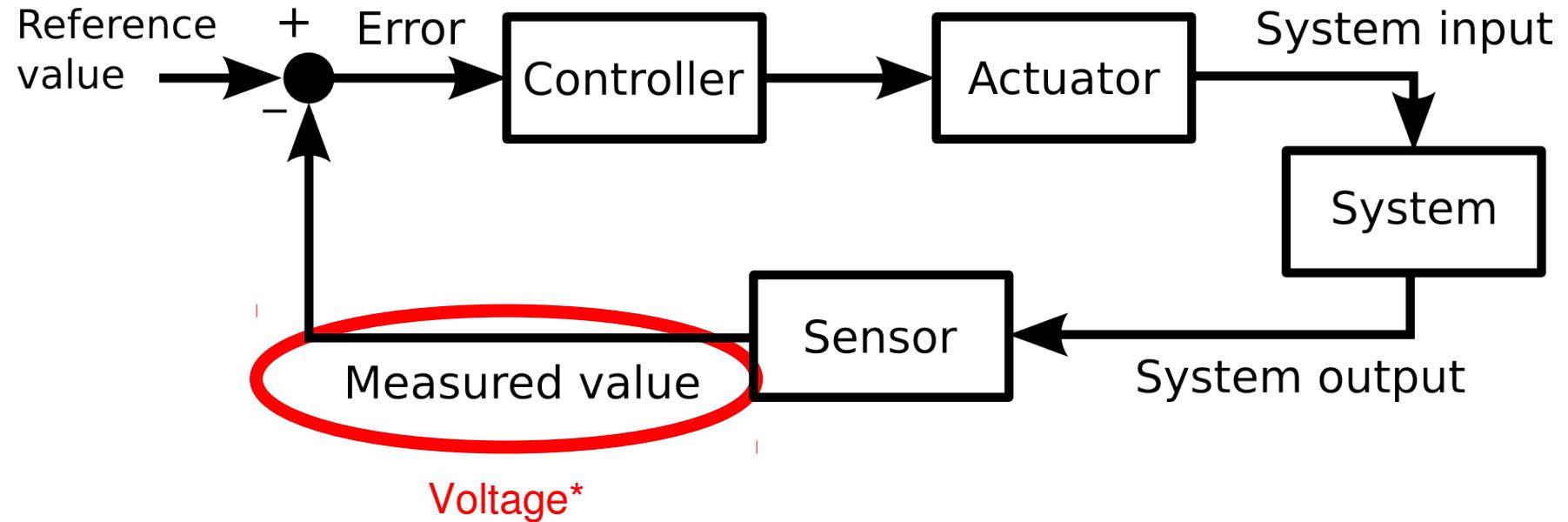
3: The sensor we use to estimate the value of the variable



# Example. Cruise control



4: The (electronic) signal containing the value of the variable

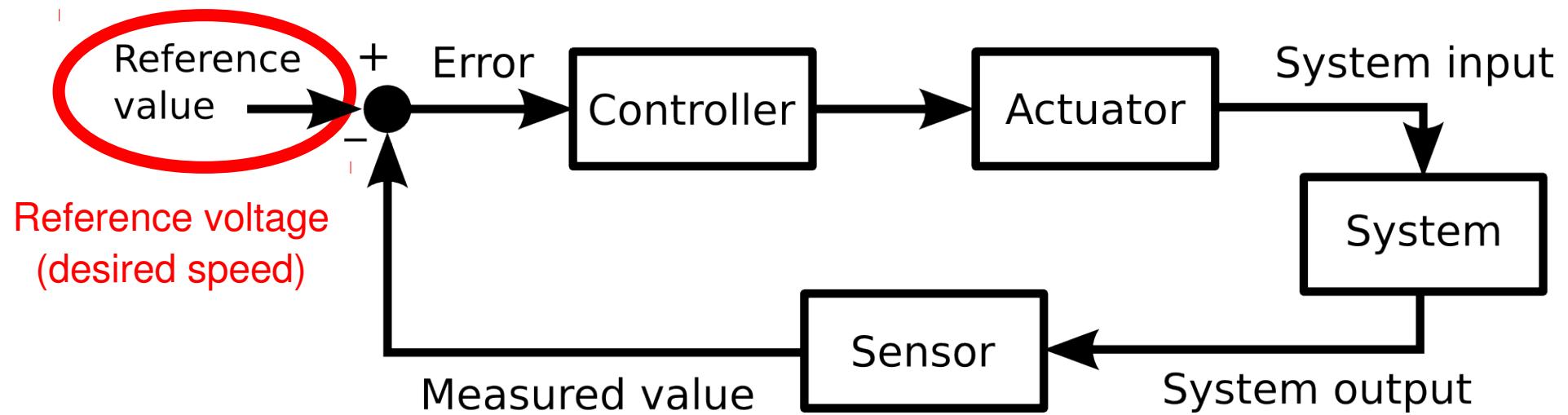


\*: Or other electronic signal unit

# Example. Cruise control



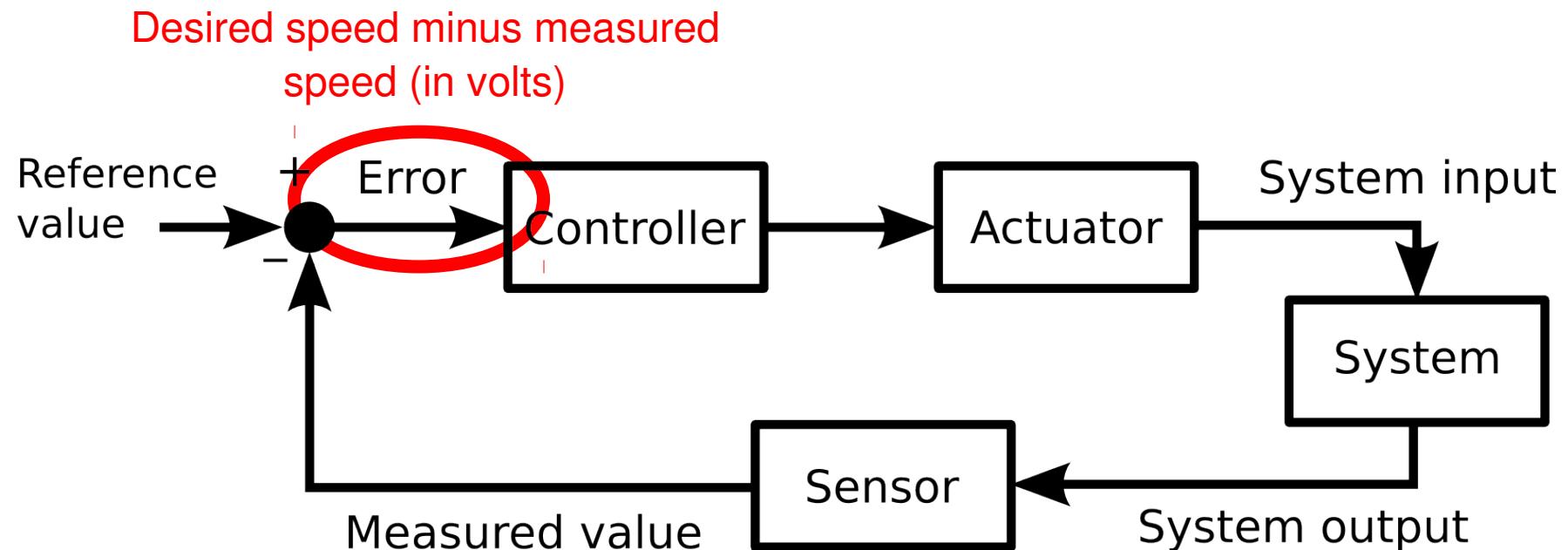
## 5: The desired value of the signal



# Example. Cruise control



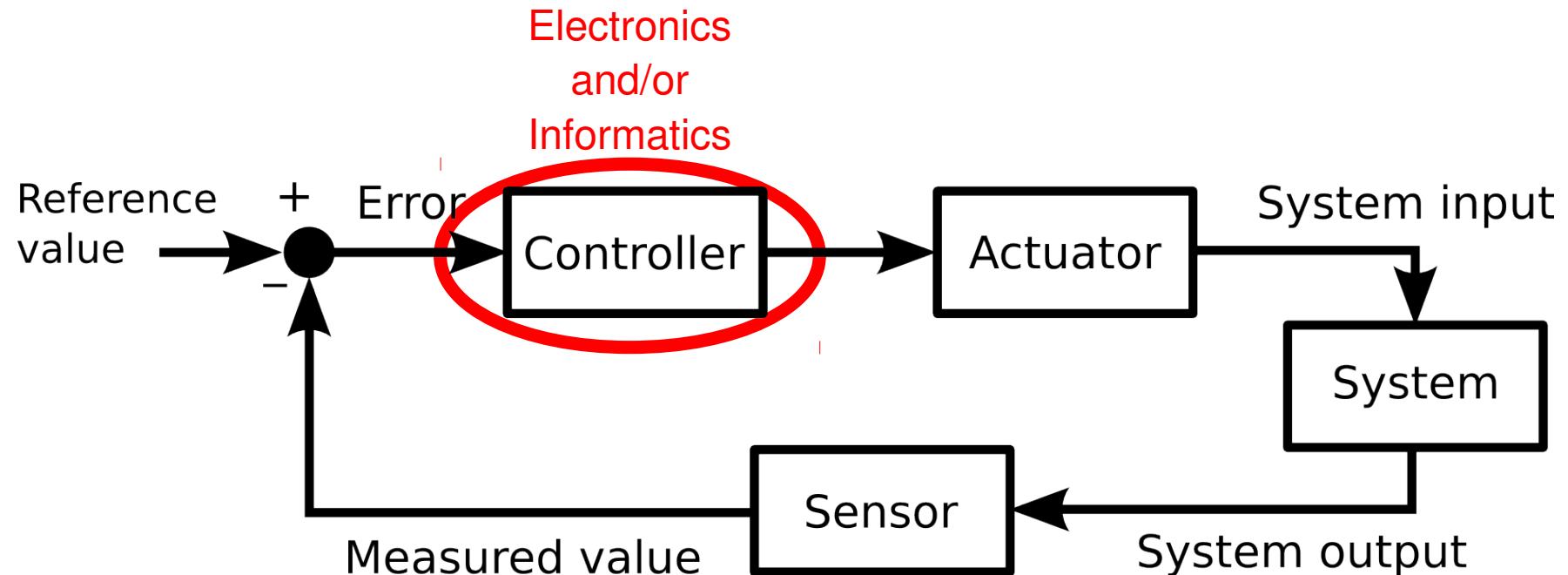
## 6: The difference between desired and actual value



# Example. Cruise control



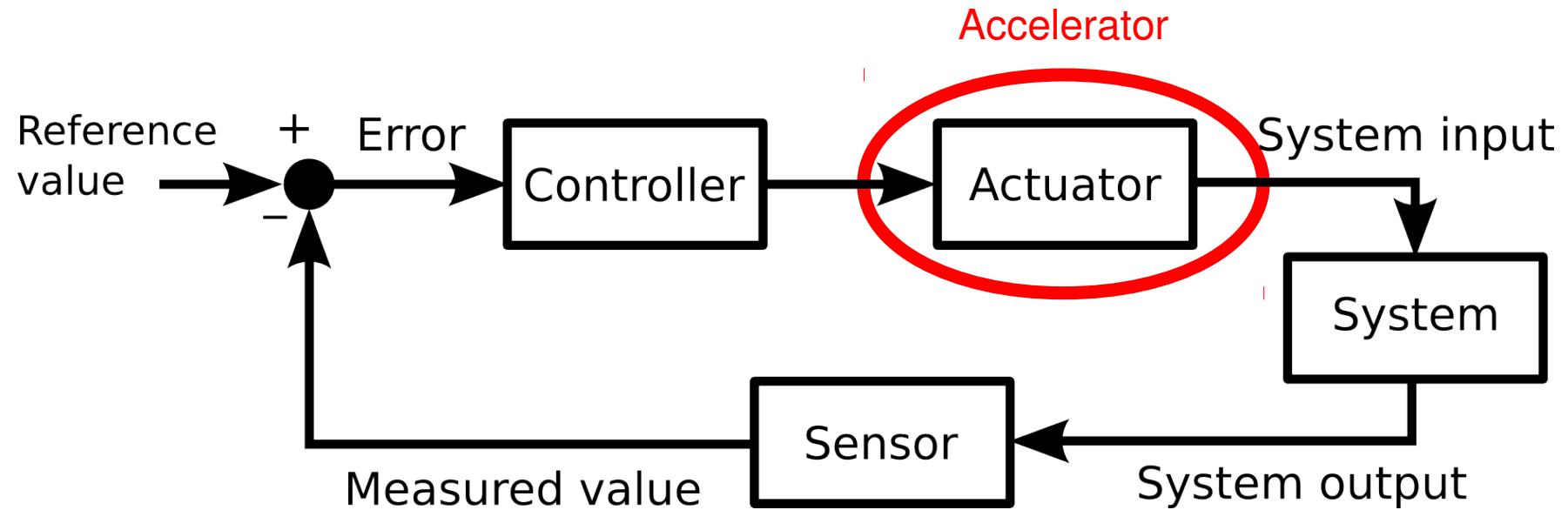
7: The controller processing the signal and taking decisions



# Example. Cruise control



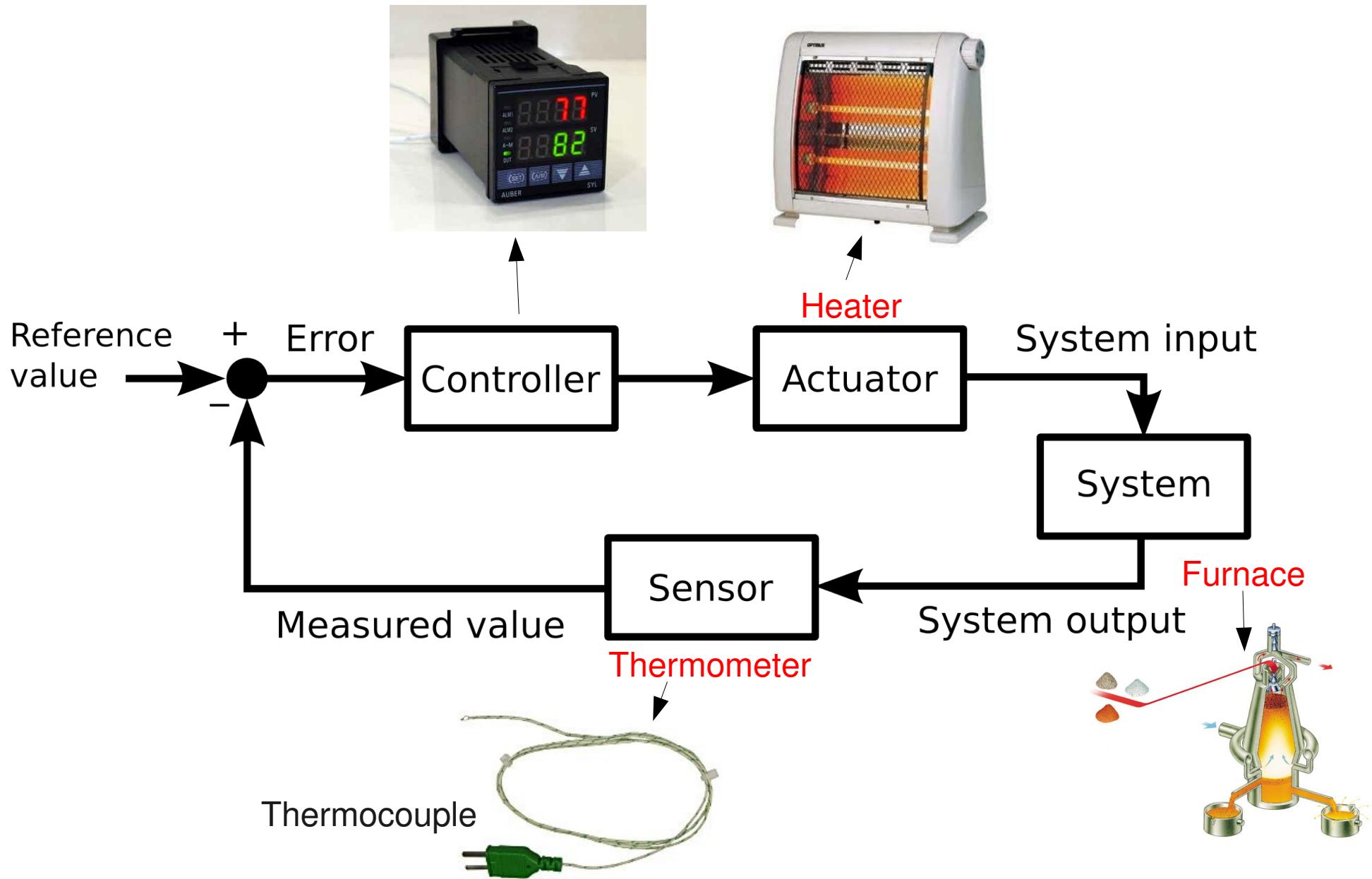
8: The transducer translating the 'decision' into an 'action'



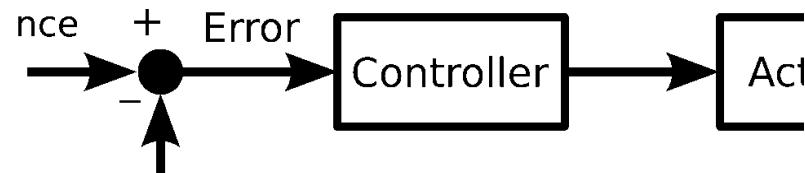
Note: system input is not same domain as system output

In this case: acceleration ( $\text{m/s}^2$ ) vs. speed ( $\text{m/s}$ )

# Example: Temperature control



# ON/OFF. Air conditioning



Simplest controller algorithm: ON/OFF:

- Switch **on** air-conditioning when it is too warm,  $Error(t) > 0$
- Switch **off** when it is too cold,  $Error(t) < 0$

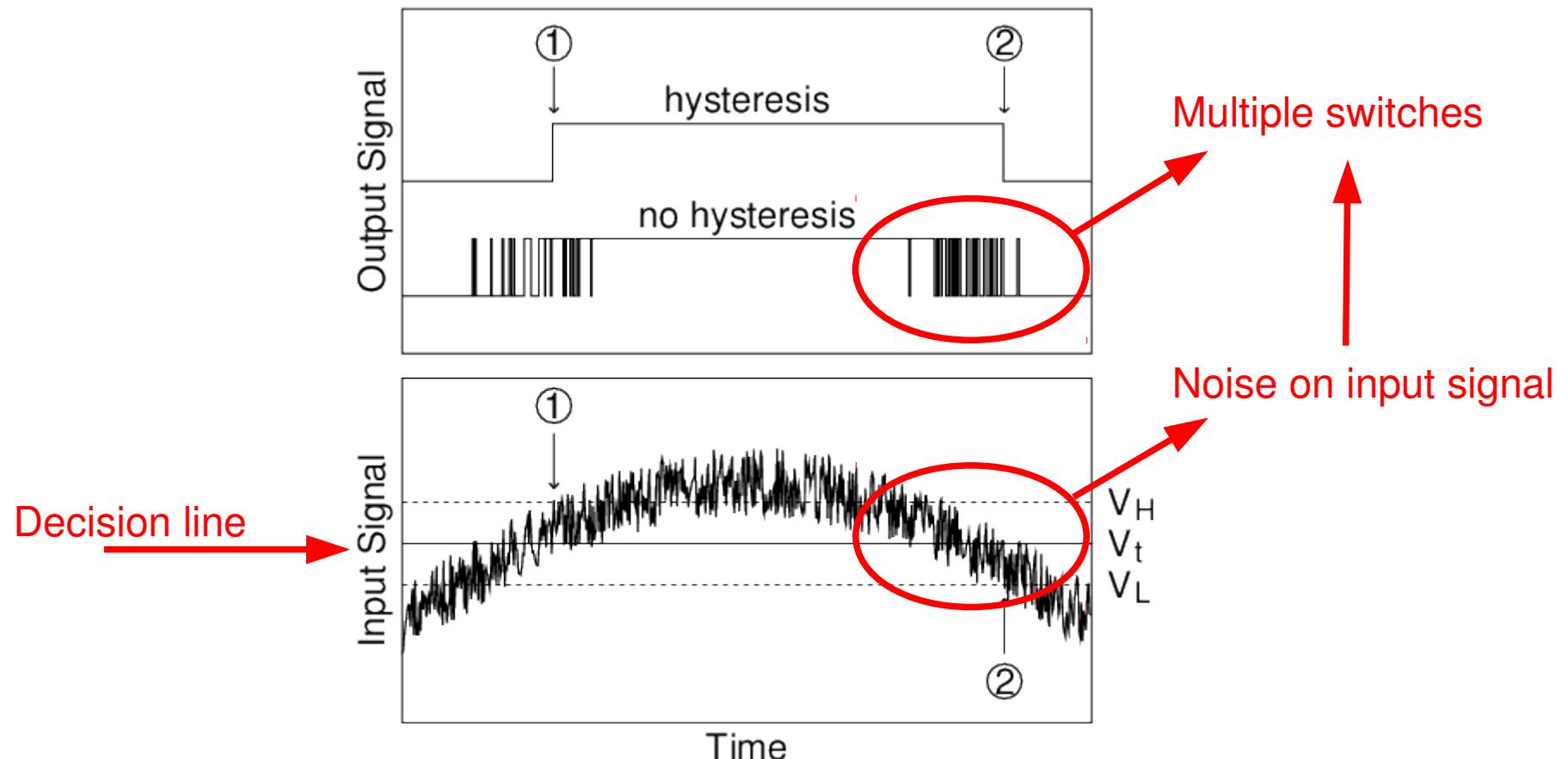




# ON/OFF. Multiple switches

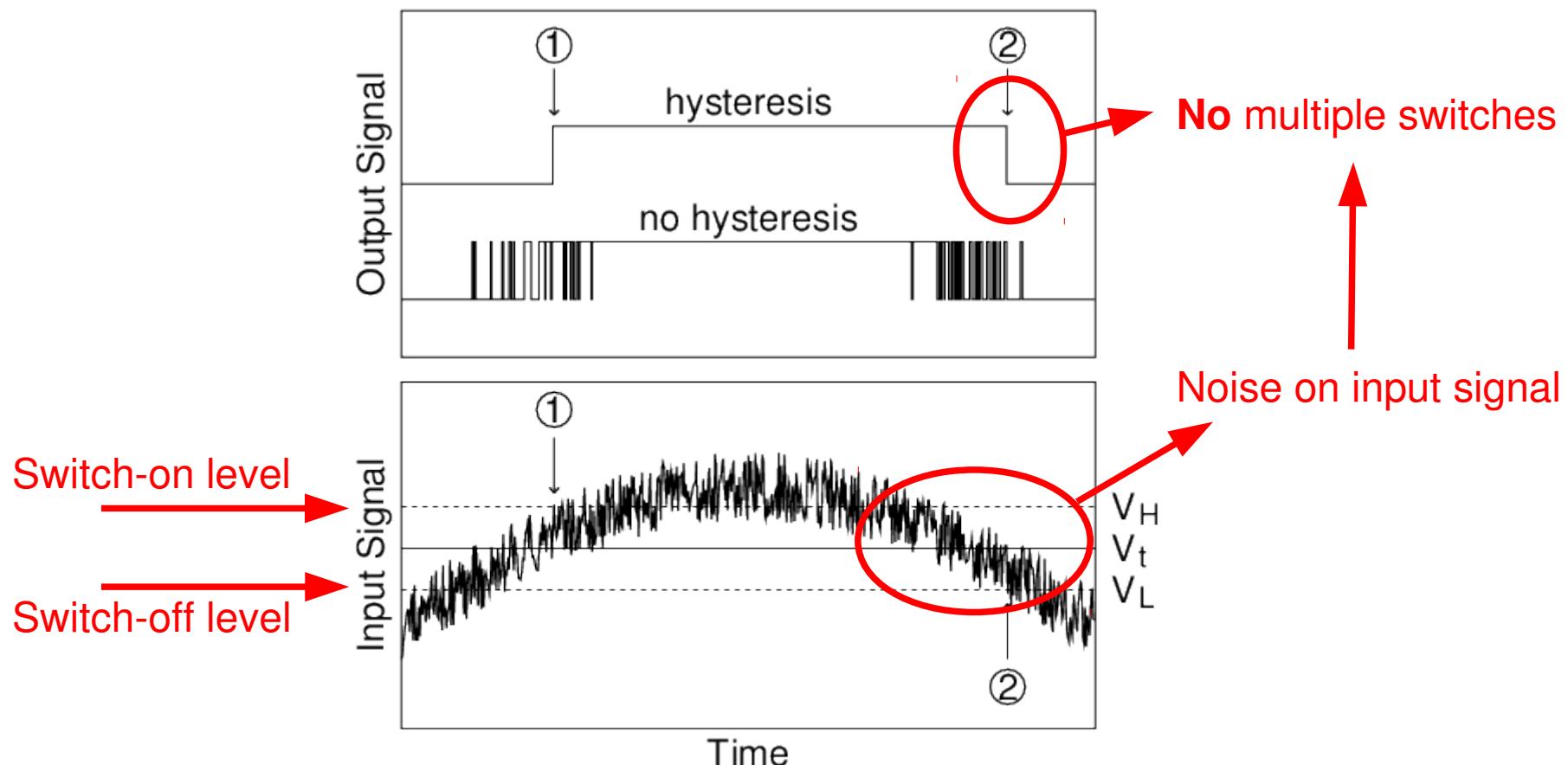
Simplest control algorithm: ON/OFF

Will cause 'switching effects':



# ON/OFF. Hysteresis

Avoid multiple switches by introducing hysteresis:



# PID

Advanced control system: PID

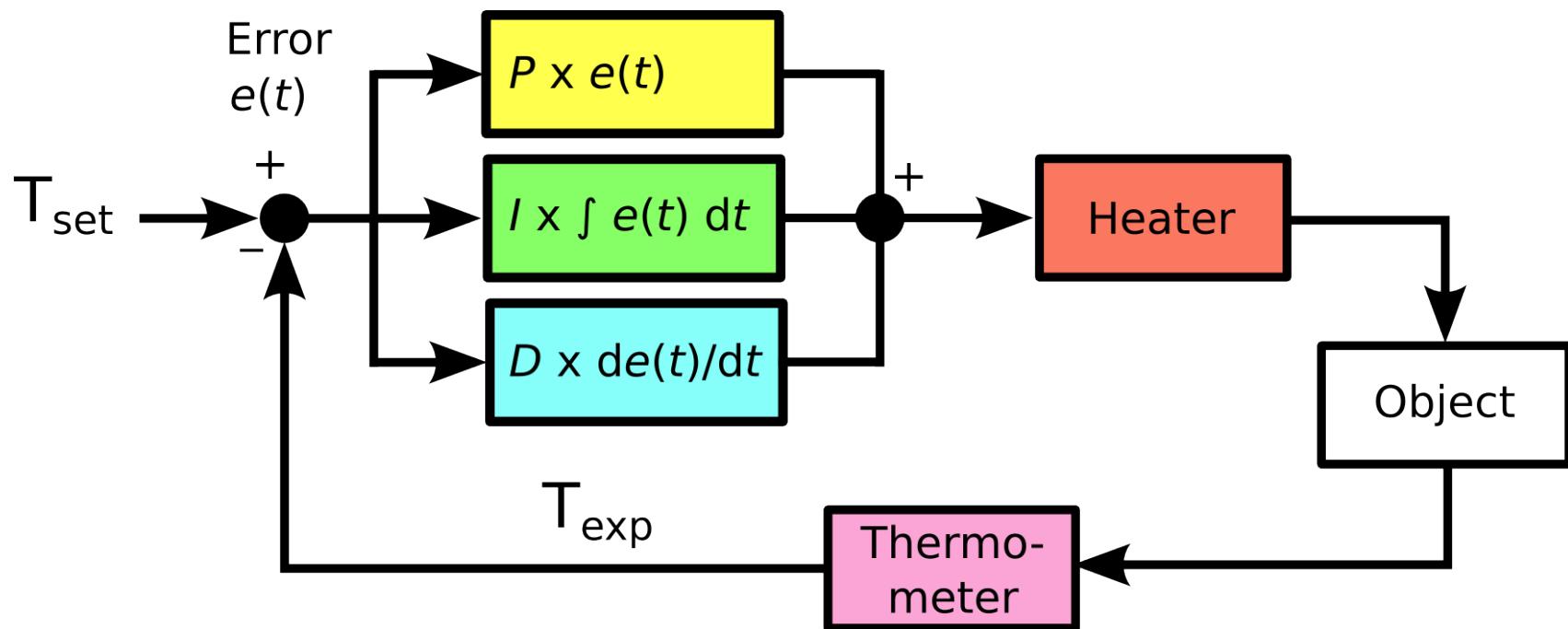
- Proportional
- Integral
- Differential



Not simple on/off binary output, but **analog scale output**

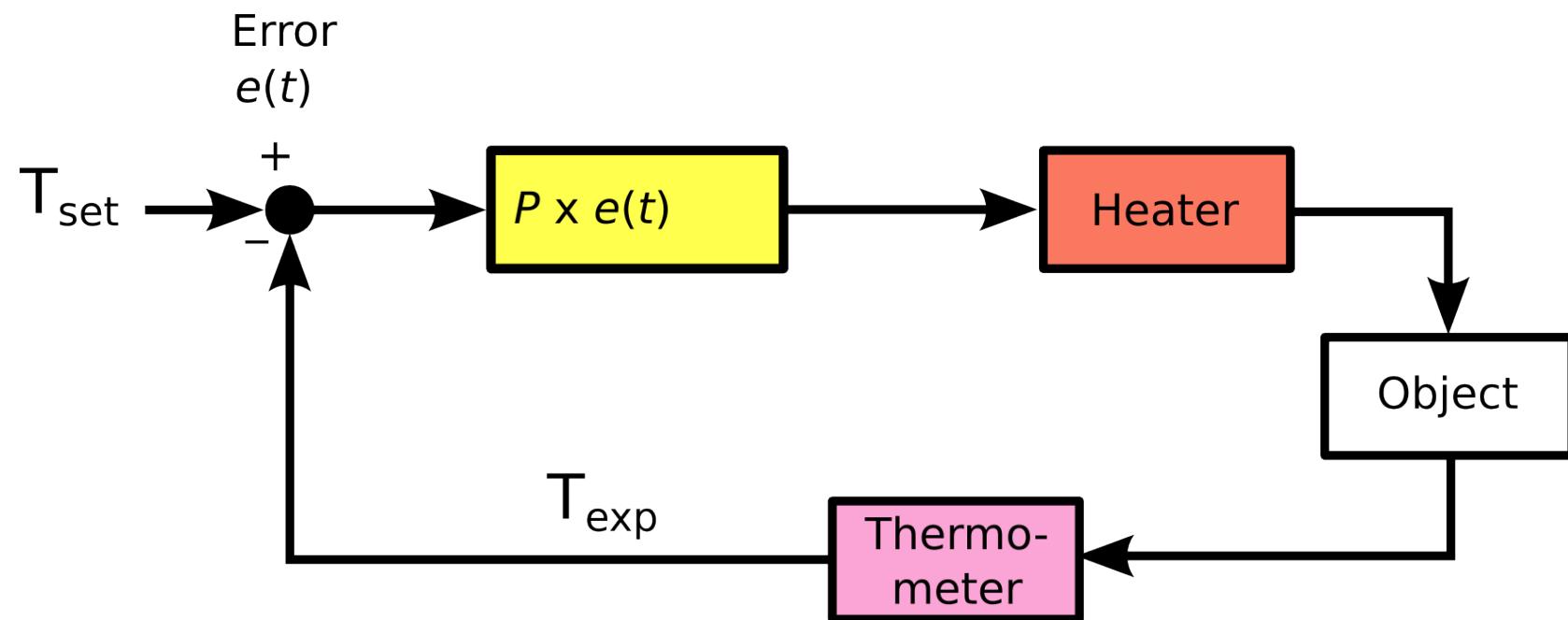
# PID

The most famous control 'algorithm/system' is PID (proportional, integral, differential). For example to control the temperature:



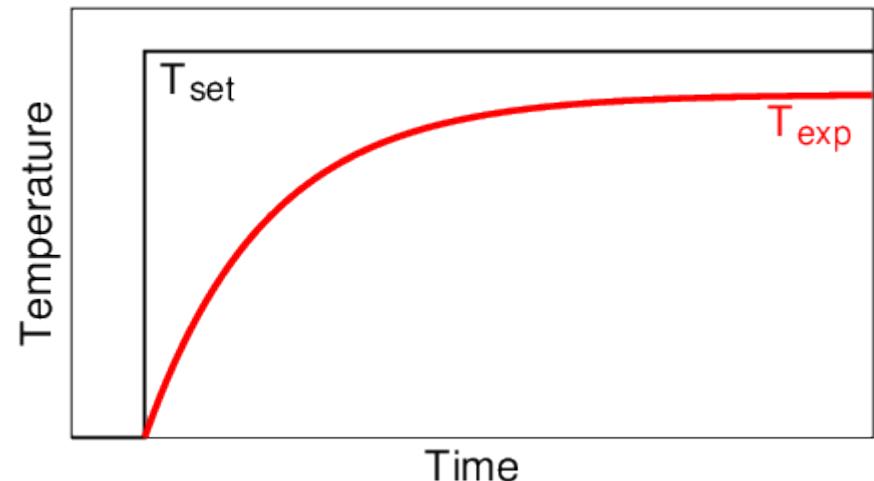
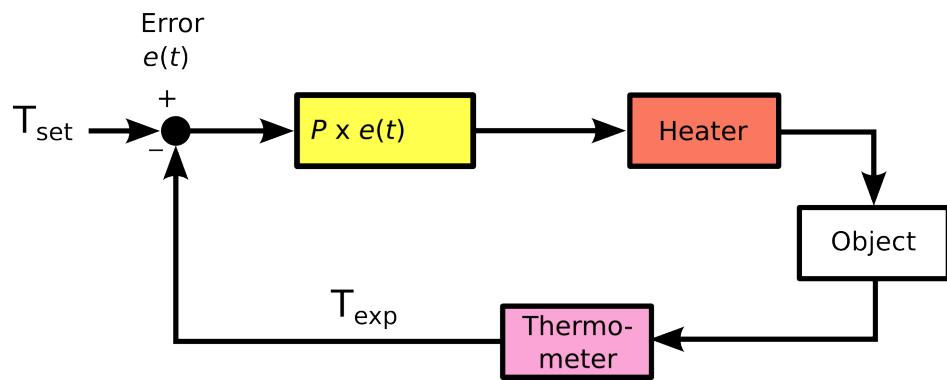
# PID: P only

P: Heater power proportional to error  $e(t) = \Delta T = T_{\text{set}} - T_{\text{exp}}$



# PID: P only

P: Cannot **ever** reach desired value  $T_{\text{set}}$  !



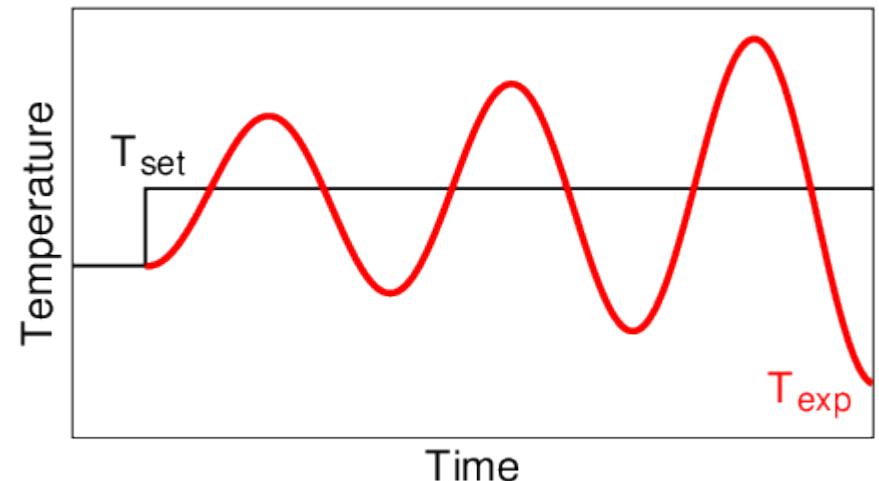
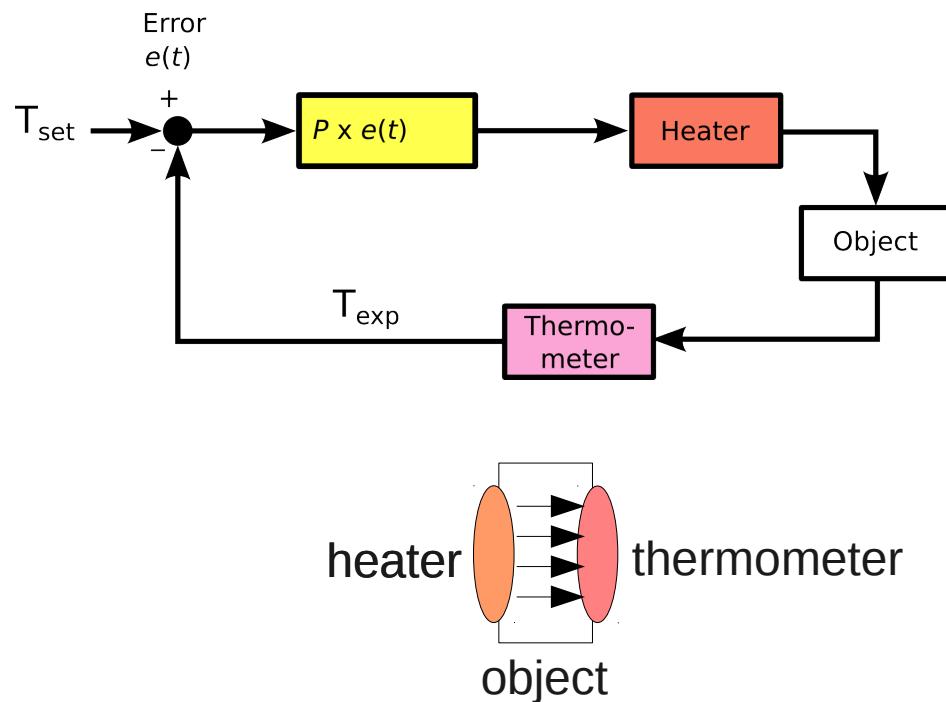
At end, 'steady state': Heater power is equal to heat loss

$$P_{\text{loss}} = P_{\text{heat}} = P \times e = P \times (T_{\text{set}} - T_{\text{exp}})$$

$$\rightarrow T_{\text{exp}} = T_{\text{set}} - P_{\text{loss}}/P$$

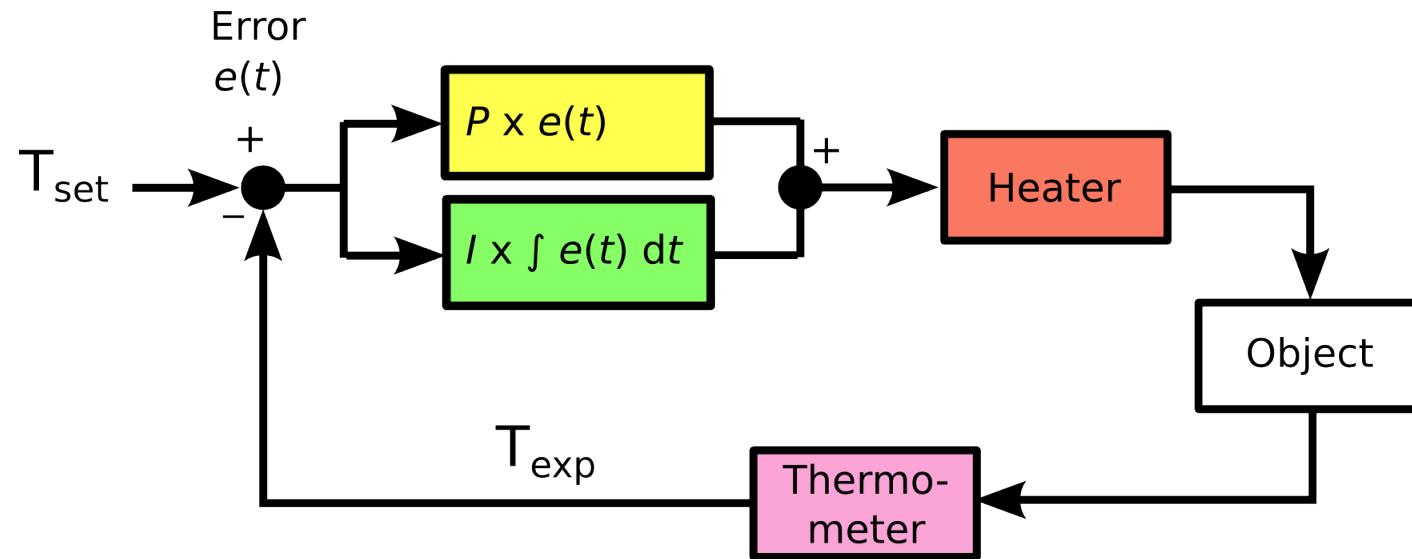
# PID: P only

P: Delay can cause oscillations



Delays ( $\Delta t$  of one loop): switches on/off the heater too late  
Can cause a run-away situation!

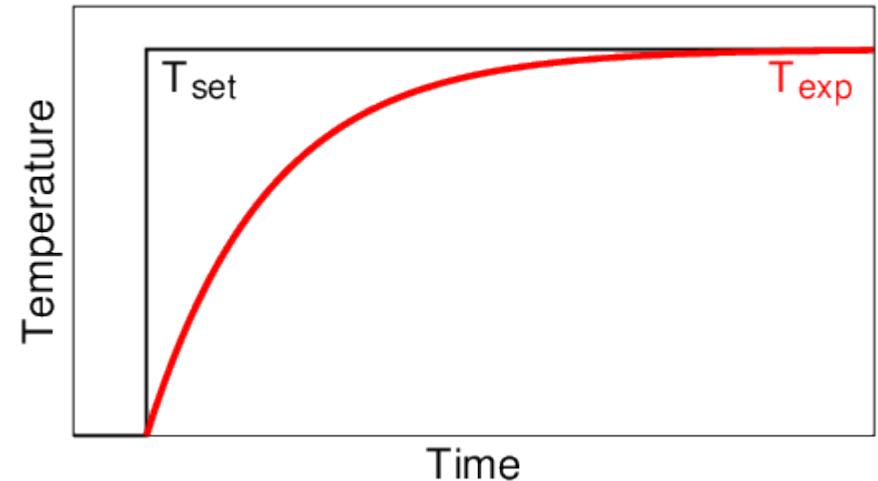
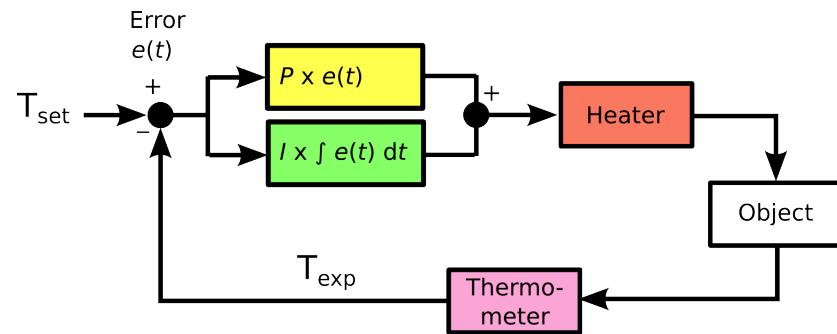
## PI: Proportional and Integral



\*: Or oscillations

# PID: PI

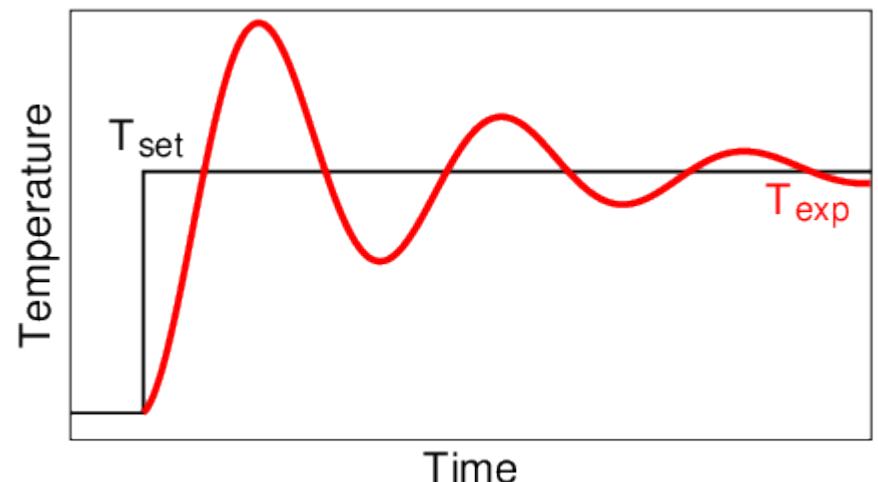
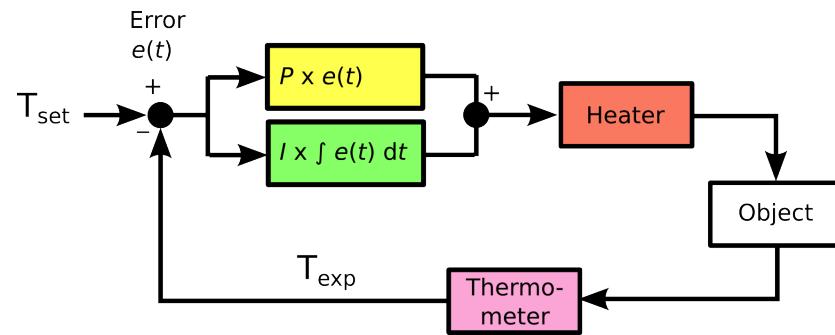
PI: Persistent errors cannot exist



If persistent error  $e(t) = e$ , then (negative)  $I(t) = \int e(t)dt$  keeps growing constantly until  $e$  disappears. Ergo: final  $e$  **must** be 0\*.

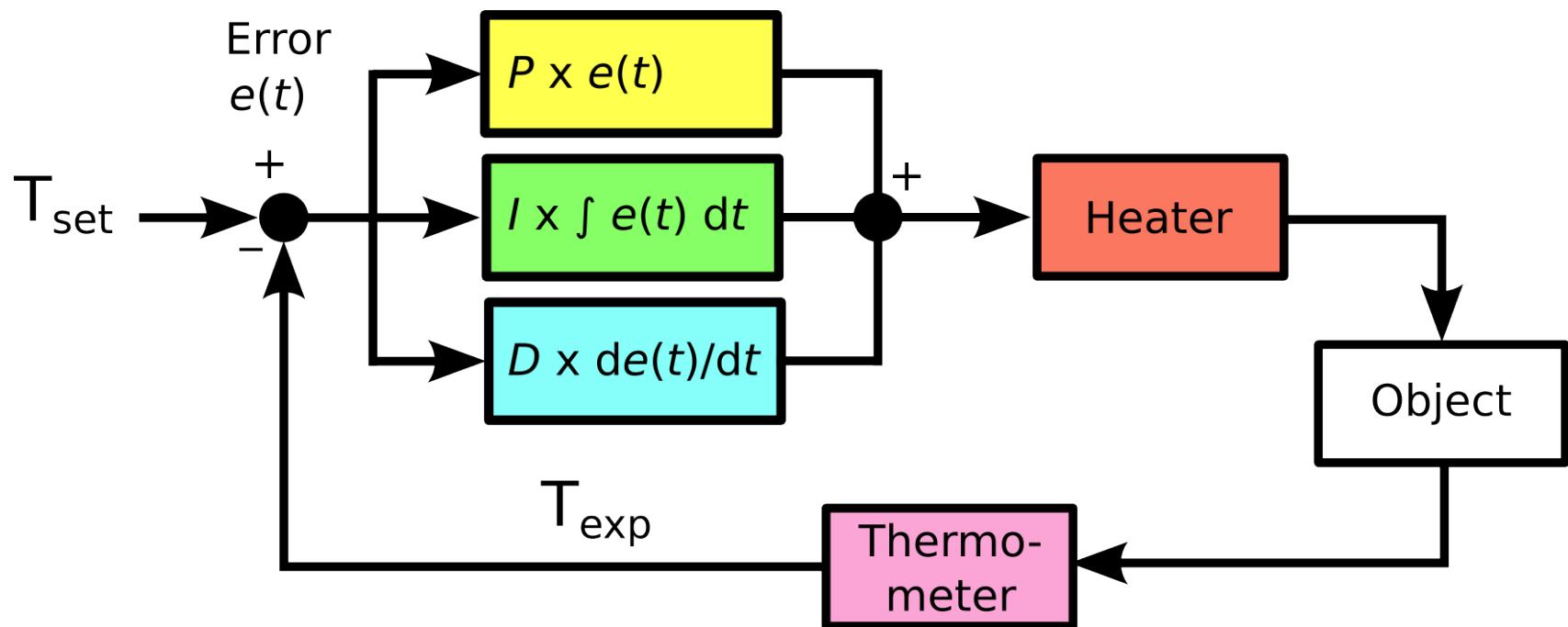
\*: Or oscillations

PI: can show severe '**overshoot**' effects



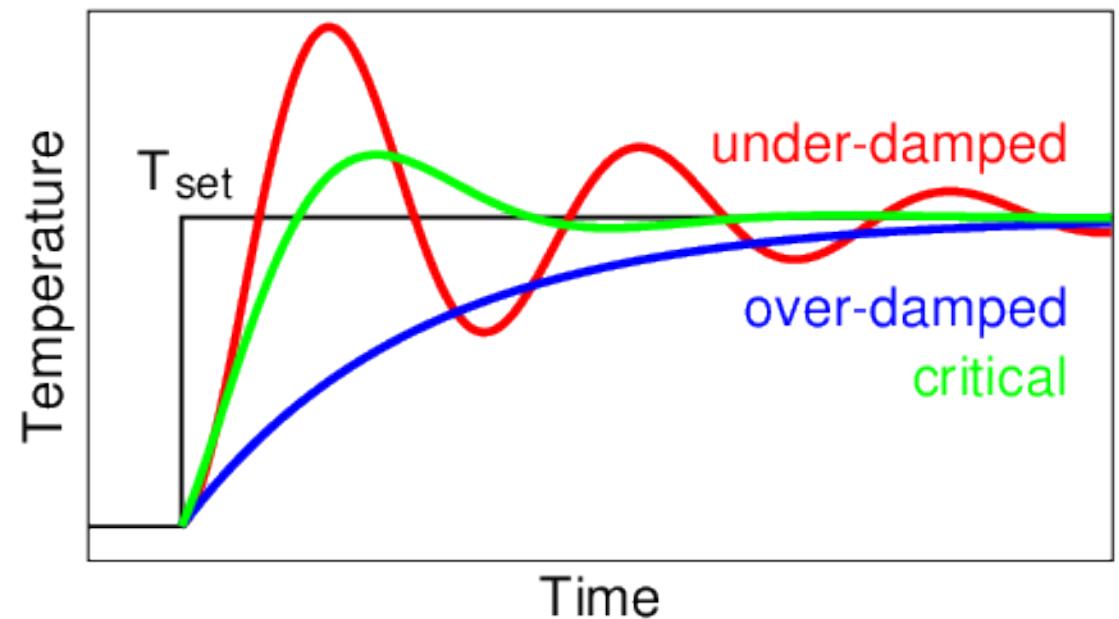
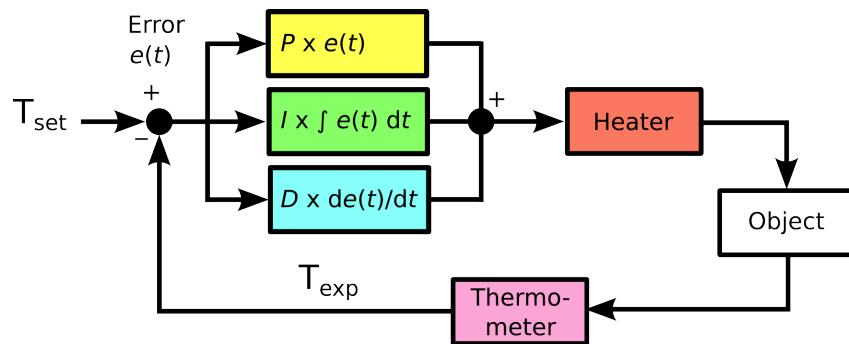
# PID. The full Monty

## The full Monty



# PID. Critical parameters

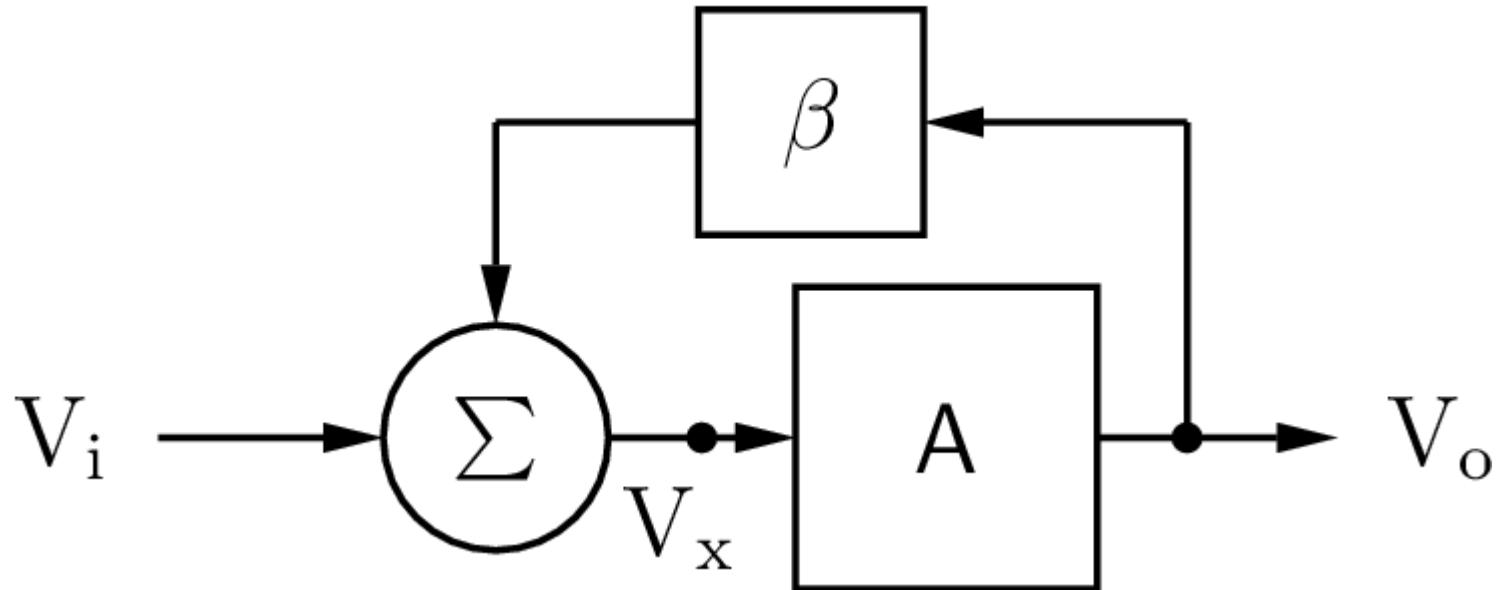
PID. By correct choice of parameters  $P$ ,  $I$  and  $D$ , we can have a system that rapidly goes to desired value



# Feedback

PID and control in general is a system of feedback:

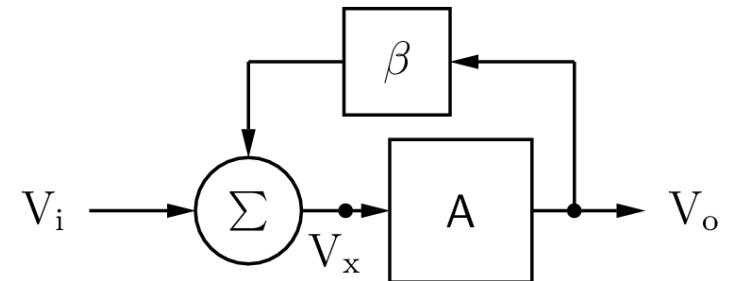
Part ( $\beta$ ) of output signal  $V_o$  is fed back (added) to input  $V_i$



Such systems can have very many aspects

- Stability (will our temperature be stable?). Positive feedback is normally unstable (oscillations or runaway signal)
  - Gain  $V_o/V_i$
  - Frequency response
- Etc. ( $\rightarrow$  Electronics II)

# Control/Feedback



Such systems find applications in many areas

- **Engineering.** Controlling temperature
- Managing the **economy** (viz. Keynes vs. Friedman, i.e., the phase of the feedback factor  $\beta$ )
- Personal **finance**. Spend less when you have less money.
- **Sociology** (a.k.a. 'training'). Put 'bad elements' in prison
- **Pedagogy** (a.k.a. 'learning'). Higher marks motivate students
- **Climatology**. Positive feedback: polar caps melt  $\rightarrow$  darker  $\rightarrow$  more heat absorption  $\rightarrow$  hotter  $\rightarrow$  etc. Negative feedback: Hotter Earth radiates more heat

Etc.