

Determine the feedback ratio $\beta = \frac{V_n}{V_0}$

(1) The right amplifier, A2 : constant mode

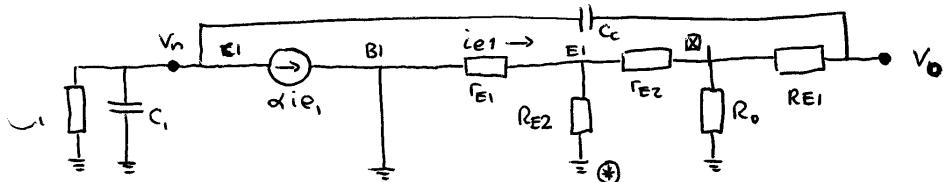
$$i_{ref} = \text{constant} = \frac{V_{ref}}{R_{ref}}$$

$$V_r = \text{constant}$$

(2) small signal analysis

- voltage source \Rightarrow ground \otimes

- current source \Rightarrow open circuit \boxtimes



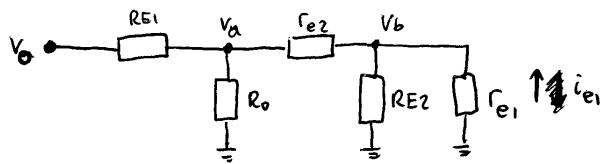
determine i_{e1} :

$$i_{e1} = -V_n \cdot R_{eq}$$

$$i_{ref} = \frac{V_{ref}}{R_{ref}} = \frac{10 \text{ V}}{1 \text{ k}\Omega} = 10 \text{ mA}, \quad r_{E2} = \frac{V_T}{i_{ref}} = \frac{26 \text{ mV}}{10 \text{ mA}} = 2.6 \text{ }\Omega$$

$$\text{max } i_1 = \frac{V_{max}}{R_1} = \frac{10 \text{ V}}{1 \text{ k}\Omega} = 10 \text{ mA}, \quad r_{E1} = 2.6 \text{ }\Omega$$

(2)
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$$\begin{aligned} R_{E1} &= 10 \text{ k} \\ R_{E2} &= 10 \text{ k} \\ R_o &= 10 \text{ k} \\ r_{e1} &= r_{e2} = 2.6 \text{ m}\Omega \end{aligned}$$

$$V_a = V_0 \cdot \frac{R_x}{R_x + R_{E1}}, \quad R_x = R_o // (r_{e2} + R_{E2} // r_{e1})$$

$$\begin{aligned} R_x &= 10 \text{ k} // (2.6 \text{ m}\Omega + 10 \text{ k} // 2.6 \text{ m}\Omega) \\ &= 10 \text{ k} // 5.2 \text{ m}\Omega \\ &= 5.2 \text{ m}\Omega \end{aligned}$$

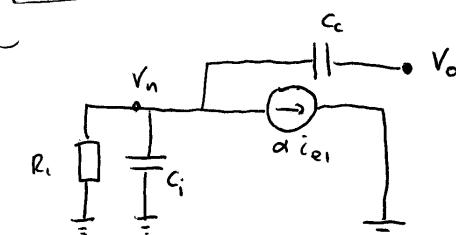
$$V_a = V_0 \cdot \frac{5.2}{5.2 + 10 \text{ k}} = 5.2 \cdot 10^{-4} V_0$$

$$V_b = V_a \cdot \frac{R_y}{R_y + r_{e2}}, \quad R_y = R_{E2} // r_{e1} \approx r_{e1} = 2.6 \text{ m}\Omega$$

$$\begin{aligned} V_b &= V_a \cdot \frac{2.6}{2.6 + 2.6} = 0.5 V_a = 0.5 \times 5.2 \cdot 10^{-4} V_0 \\ &= 2.6 \cdot 10^{-4} V_0 \end{aligned}$$

$$V_b \approx \frac{r_{e1}}{R_{E1}} \cdot V_n$$

$$i_{e1} = -\frac{V_b}{r_{e1}} = -\frac{V_0}{R_{E1}}$$



$$\text{In } V_n: \sum I = 0$$

$$V_n \left(\frac{1}{R_1} + sC_1 \right) + (V_n - V_o) sC_c - V_o \frac{1}{R_{E1}} = 0$$

$$\beta = \frac{V_n}{V_o} = \frac{\frac{1}{R_{E1}} + sC_c}{\frac{1}{R_1} + sC_1 + sC_c} = \frac{\frac{R_1}{R_{E1}}}{1 + sR_1(C_1 + C_c)}$$

$$R_1 = 1 \text{ k}\Omega$$

$$C_1 = 10 \text{ pF}$$

$$C_c = 1 \text{ nF}$$

$$R_{E1} = 10 \text{ k}\Omega$$

$$\beta_0 = 0.1$$

pole at

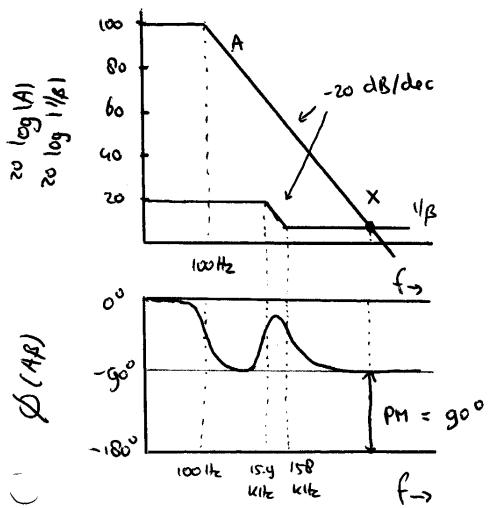
$$f_p = \frac{1}{2\pi R_1(C_1 + C_c)} \quad f_0 = \frac{1}{2\pi R_{E1}C_c}$$

$$158 \text{ kHz}$$

$$15.8 \text{ kHz}$$

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$$\beta = \frac{R_i}{R_{E1}} \cdot \frac{1 + s R_{E1} C_c}{1 + s R_i (C_i + C_c)}$$

$$\beta(f=0) = \frac{R_i}{R_{E1}} = 0.1$$

$$\beta(f=\infty) = \frac{R_i}{R_{E1}} \cdot \frac{R_{E1} C_c}{R_i (C_i + C_c)} \approx 1$$

f_x :

$$|A| = \frac{A_0}{(1 + f_x/f_p)} \approx A_0 \frac{f_p}{f_x}$$

$$\text{From } X: |A| = |\beta(f=\infty)|$$

$$A_0 \frac{f_p}{f_x} = \beta_\infty = 1 \Rightarrow f_x = A_0 f_p \\ = 10^7 \text{ Hz} = 10 \text{ MHz}$$

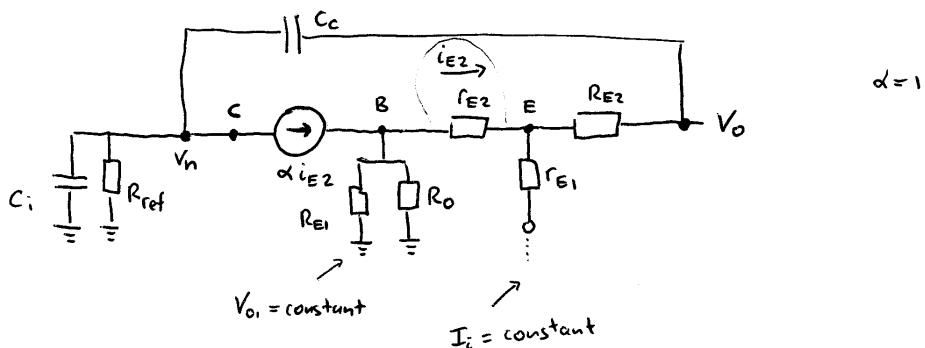
In reality, this circuit is probably not stable due to the fact that the OpAmp will have more poles before 10 MHz.

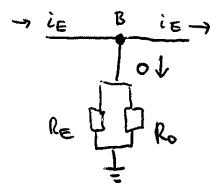
stability of right part of circuit

left amplifier A1 constant mode

$$i_i = \text{constant} (= V_{max}/R_i)$$

V_o = constant



Kirchov in B ($\alpha = 1$)No current through $R_E \parallel R_o \Rightarrow V_B = 0 \text{ V}$

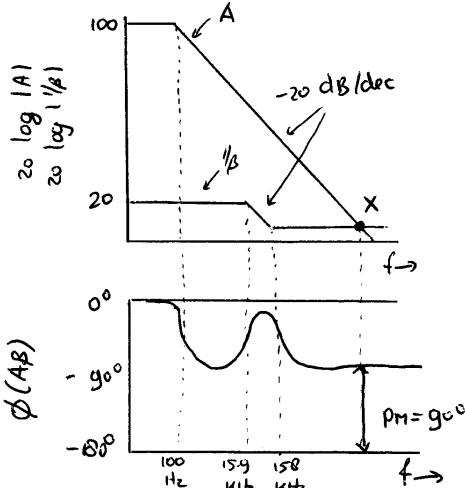
$$i_{E2} = \frac{V_B - V_o}{R_{E2} + r_{E2}} = -\frac{V_o}{R_{E2}' + r_{E2}} = -\frac{V_o}{R_{E2}'}$$

$$\sum I_n = V_n : \sum I = 0$$

$$V_n \left(\frac{1}{R_{ref}} + sC_i \right) + \alpha i_{E2} + sC_c (V_n - V_o) = 0$$

$$V_n \left(\frac{1}{R_{ref}} + sC_i \right) - V_o \left(\frac{1}{R_E'} \right) + sC_c (V_n - V_o) = 0$$

$$\beta = \frac{V_n}{V_o} = \frac{\frac{1}{R_E'} + sC_c}{\frac{1}{R_{ref}} + sC_i + sC_c} = \frac{R_{ref}}{R_E'} \cdot \frac{(1 + sR_E' C_c)}{(1 + sR_{ref}(C_i + C_c))}$$



$$\begin{aligned} & \text{po} \\ & \text{polo at } f_p = \frac{1}{2\pi R_{ref}(C_i + C_c)} \quad \text{zero at } f_0 = \frac{1}{2\pi R_E' C_c} \\ & \text{at } 158 \text{ kHz} \quad \text{at } 15.9 \text{ kHz} \end{aligned}$$

equal to (a)

$$\phi(A\beta)$$

