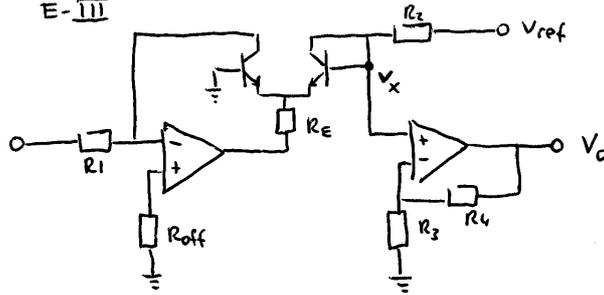


(a)



left:  $I_i = \frac{V_i}{R_1}$  ( $V_-$  is terra virtual)

$$V_{BE1} = \frac{kT}{q} \ln \frac{V_i}{R_1 \cdot I_S}$$

$$V_x = -V_{BE1} + V_{BE2}$$

$$V_{BE2} = \frac{kT}{q} \ln \frac{V_{ref}}{R_2 \cdot I_S} \quad \text{when } V_x \approx 0$$

$$V_x = \frac{kT}{q} \ln \left( \frac{V_{ref} R_1}{V_i R_2} \right)$$

ex.  $R_1 = R_2$   
 $V_i = 10$   $V_{ref} = 10$  V  
 $V_x \approx 60$  mV compare  
 $V_{ref} - V_x = 0.94$  V instead of 1 V  
 (6% error in calculation)  
 $\Delta V_x = -\frac{kT}{q} \ln 0.94 = -1.6$  mV  
 (b)  $\left| \frac{\Delta V_0}{V_0} \right| = \frac{1.6}{60} \times 100\% = 2.7\%$

$$V_0 = \frac{R_4 + R_3}{R_3} \cdot V_x$$

$$= \frac{R_4 + R_3}{R_3} \cdot \frac{kT}{q} \ln \left( \frac{V_{ref} R_1}{V_i R_2} \right) = - \frac{R_4 + R_3}{R_3} \frac{kT}{q} \ln \left( \frac{V_i R_2}{V_{ref} R_1} \right)$$

(c)  $V_0 = c \frac{T}{R_3} \quad (R_4 \gg R_3) \quad c = \frac{R_4}{q} \cdot k \quad , \quad R_3 = (144T) \cdot R_{30}$

$$\frac{dV_0}{dT} = \frac{d \left( c \frac{T}{R_3} \right)}{dT} \cdot \frac{dT}{dT} + \frac{d \left( c \frac{T}{R_3} \right)}{dR_3} \cdot \frac{dR_3}{dT}$$

$$= c \cdot \frac{1}{R_3} - c \frac{T}{R_3^2} \cdot \alpha R_3$$

$$\frac{dV_0}{dT} = 0 \Rightarrow \frac{c}{R_3} (1 - \alpha T) = 0 \Rightarrow \alpha = \frac{1}{T}$$

(d) p. 11 de Sebenta :  $R_{off} = R_1$

$V_- = V_+$  (opamp ideal)

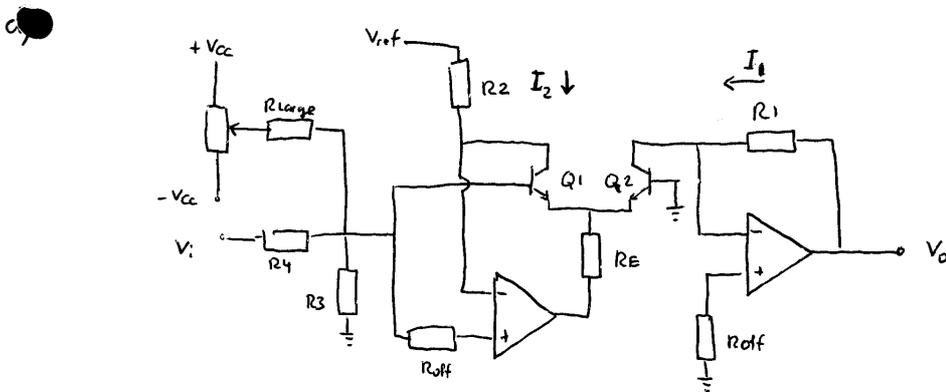
$V_- = V_+ = -R_{off} I_b$

$I_i = (V_i - V_-) / R_1 = (V_i + R_{off} I_b) / R_1$

$I_{c1} = I_i - I_b = \frac{V_i}{R_1} + \frac{R_{off}}{R_1} I_b - I_b$

$R_1 = R_{off} \Rightarrow I_{c1} = V_i / R_1$

2: amplificador ant-logartítmico (exponential)



$V_{b-1} = V_i \cdot \frac{R_3}{R_3 + R_4}$

$V_{b-1} = 0 - V_{be-2} + V_{be-1}$

$= -\frac{kT}{q} \ln \frac{I_1}{I_s} + \frac{kT}{q} \ln \frac{I_2}{I_s} = \frac{kT}{q} \ln \frac{I_2}{I_1}$

$I_1 = \frac{V_0}{R_1}, I_2 = \frac{V_{ref}}{R_2} \Rightarrow V_{b-1} = \frac{kT}{q} \ln \frac{V_{ref}}{V_0} \cdot \frac{R_1}{R_2}$

$V_i \cdot \frac{R_3}{R_3 + R_4} = \frac{kT}{q} \ln \frac{V_{ref}}{V_0} \cdot \frac{R_1}{R_2} \Rightarrow \frac{V_{ref}}{V_0} \cdot \frac{R_1}{R_2} = \exp\left(\frac{qV_i}{kT} \cdot \frac{R_3}{R_3 + R_4}\right)$

$V_0 = \frac{R_1}{R_2} V_{ref} \exp\left(-\frac{qV_i}{kT} \cdot \frac{R_3}{R_3 + R_4}\right)$

b)  $V_i = 0 \Rightarrow V_0 = \frac{R_1}{R_2} V_{ref}$  . teóricamente  
 para  $V_i = 0$  , ajustar o potenciometro até que  $V_0 = \frac{R_1}{R_2} V_{ref}$